## PIT: Optimization of Dynamic Sparse Deep Learning Models via Permutation Invariant Transformation

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Microsoft Research



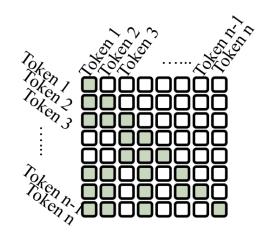


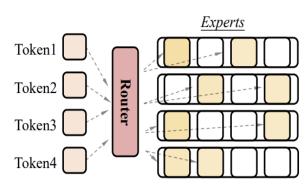


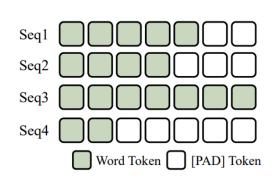


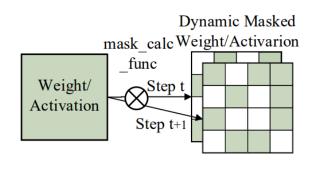
### Dynamic Sparsity in Deep Learning Models

- Dynamic sparsity commonly exists in modern deep learning models (e.g., LLM), which spans in both
  - Weight tensors (pruned models) and activation tensors (sparse attention)
  - Input data (varying seq. length) and model architectures (MoE)
  - Training and inference









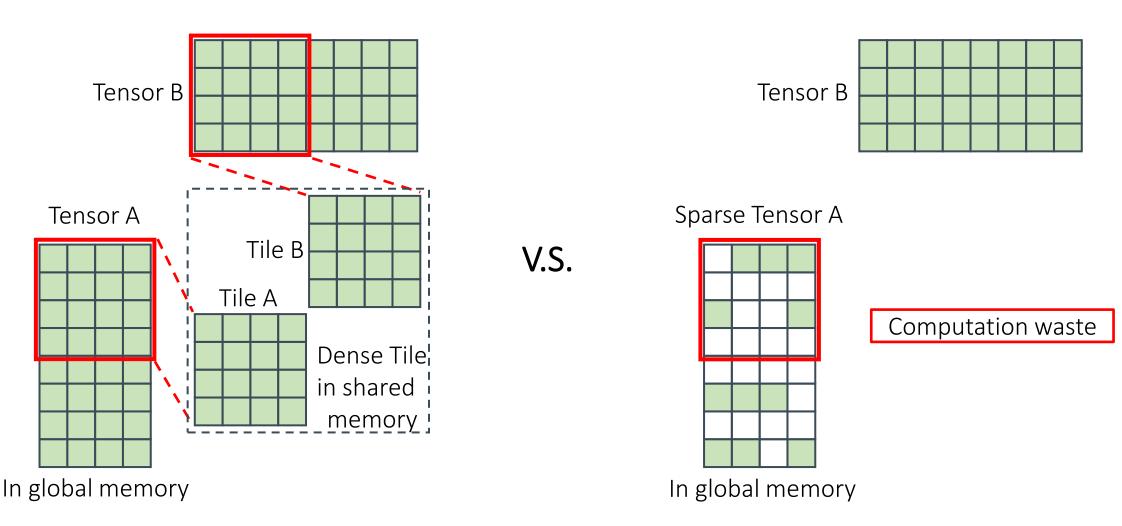
Dynamic Sparse Attention

Mixture-of-Experts (MoE)

Dynamic sequence length

**Sparse Training** 

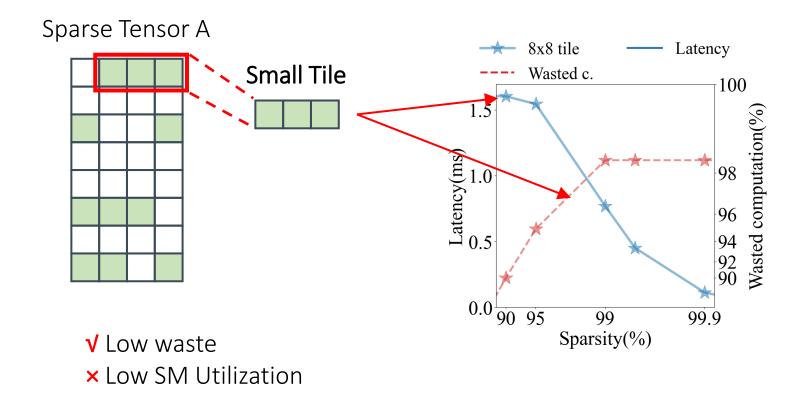
### Dynamic Sparsity Hardly Aligned to Accelerators



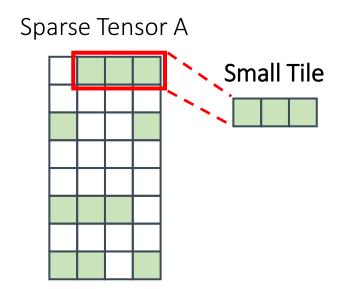
Dense Matrix Multiplication C=A·B

Sparse Matrix Multiplication C=A·B

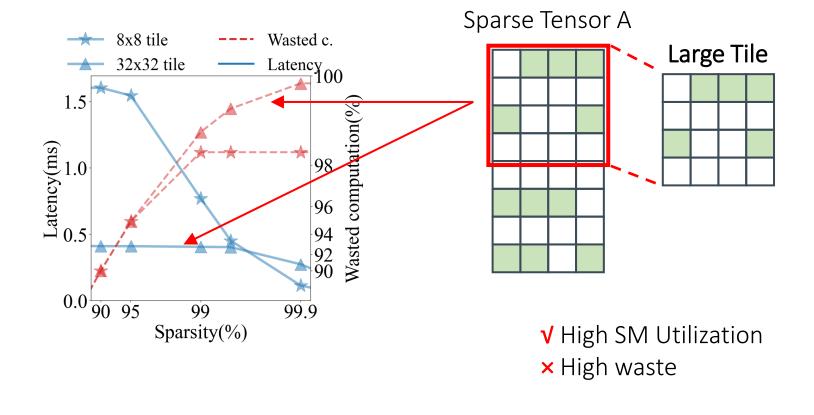
### Dilemma of Tile Covering



## Dilemma of Tile Covering

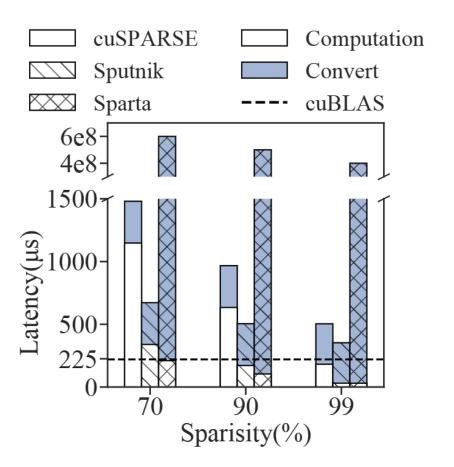


- **V** Low waste
- **★** Low SM Utilization



### Sparsity-Aware Kernels?

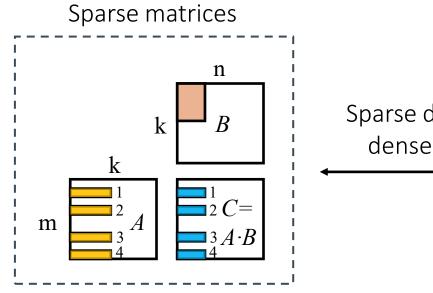
- Build fine-grained index (e.g., CSR) to skip computation
- Significant overhead during index construction and data access
- Worse than the dense counterpart



#### - We want to achieve:

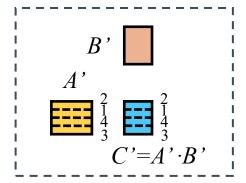
- Use computation-efficient large tiles,
- With low computation waste,
- With minimal data conversion and access overhead.

### Opportunity: Sparse-to-Dense Transformation



Sparse data in A rearranged to dense data A along m-axis

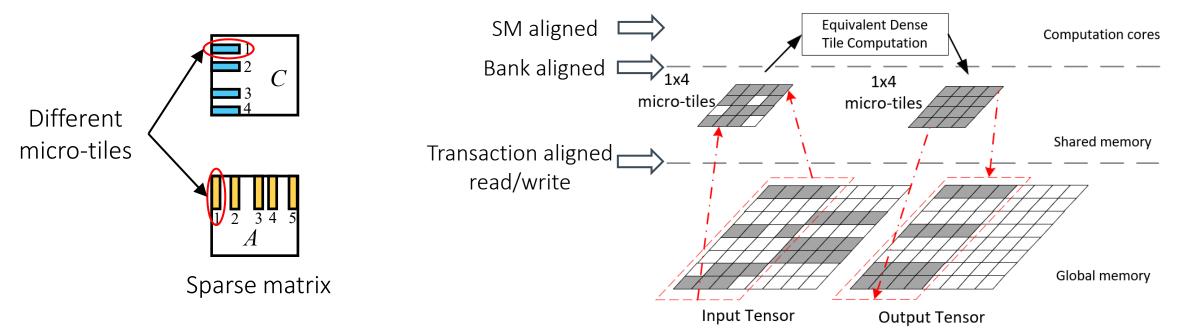
Dense tile computation



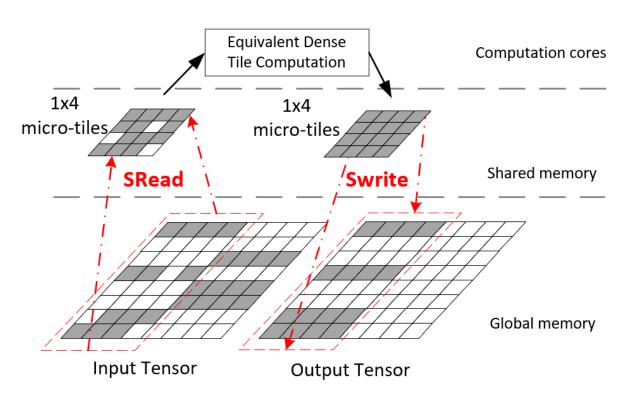
- Data rearrangement does not affect dense computation
- The rearrangement can be out-of-order

#### Micro-tile

- -- The minimal granularity of rearrangement
- Micro-tile is a small data unit aligned with the hardware read/write granularity of an accelerator (e.g., GPU)
  - Read/write transaction is as small as 32 bytes in CUDA GPUs
  - Enable aligning to every level of an accelerator, e.g., global memory, shared memory, computation instructions



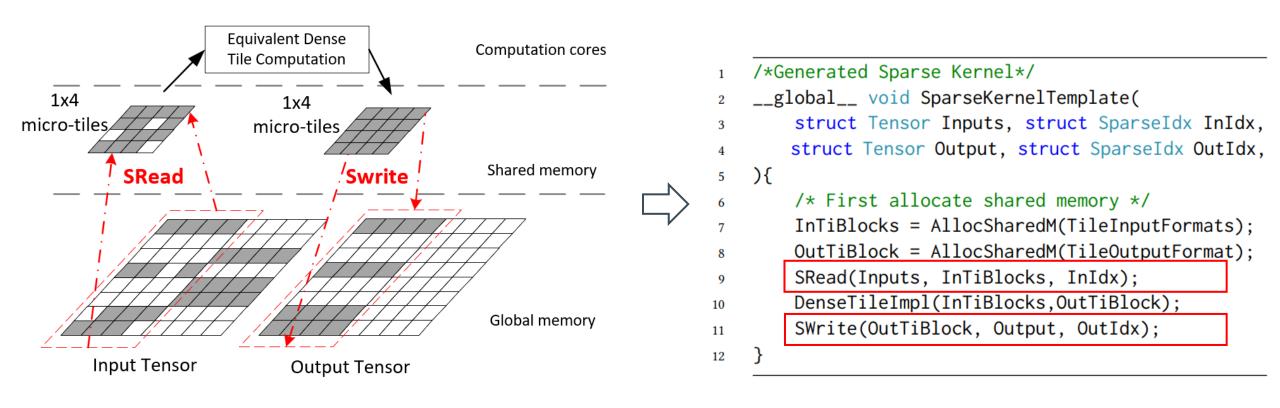
#### SRead and SWrite Primitives



- Rearrangement piggybacked during data movement across memory hierarchies
- Random access with zero cost due to aligned data granularity (i.e., micro-tile)

SRead and SWrite do **online rearrangement** of micro-tiles

#### SRead and SWrite Primitives



SRead and SWrite do online rearrangement of micro-tiles

The sparse kernel template in PIT

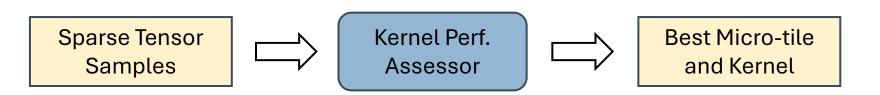
#### Permutation Invariant Transformation

- An axis of an einsum notation is **PIT-axis** if and only if any shuffling of data on this axis does not affect the correctness of the operator
  - All the computations on a PIT-axis are commutative and associative

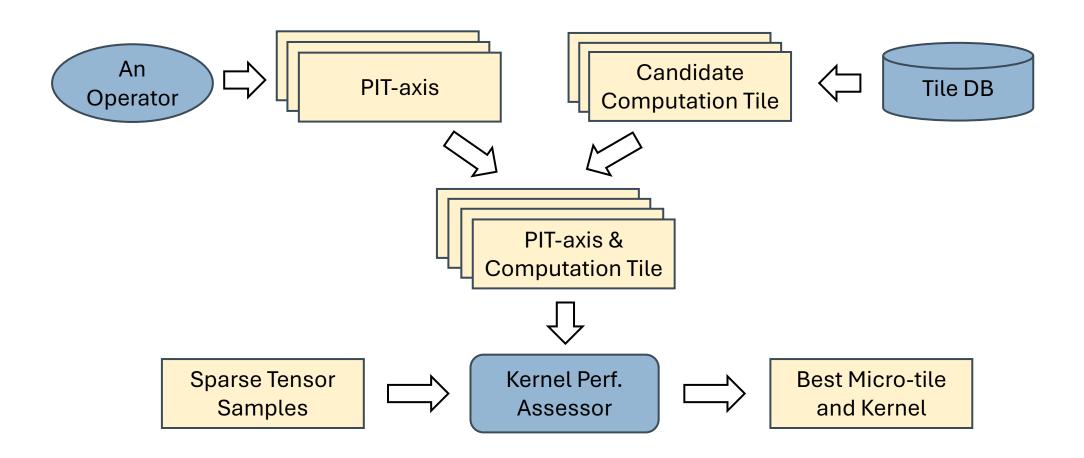
Operator	Tensor Expression	PIT-axis	not PIT-axis
ReduceSum	C[p] += A[p, l]	p, l	
Vector Addition	C[p] = A[p] + B[p]	p	
MatMul	C[m,n] += A[m,k]*B[k,n]	m, n, k	
BatchMatMul	C[b, m, n] += A[b, m, k] *B[b, k, n]	b, m, n, k	
Convolution	C[n, f, x, y] +=	n, m, f	x, y, i, j
	$A[n, m, x+i, y+j]^*B[f, m, i, j]$		

A PIT rule contains the combination of a PIT-axis, a micro-tile shape, and a dense computation tile.

### Micro-tile Selection for Kernel Construction

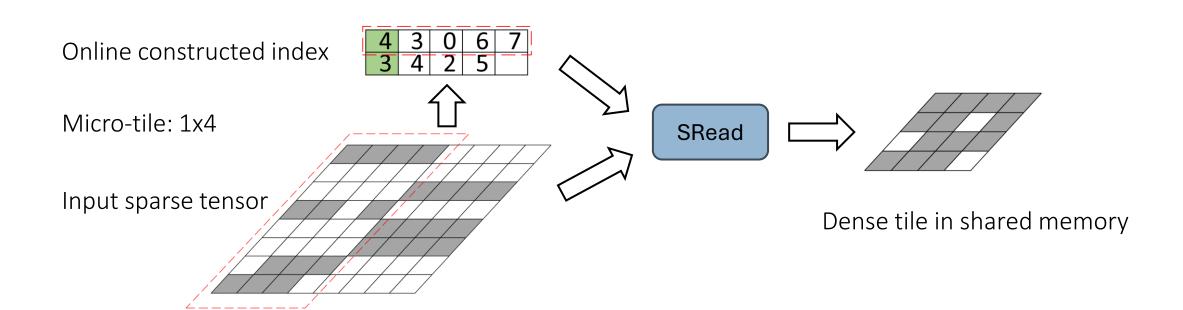


## Micro-tile Selection for Kernel Compiling

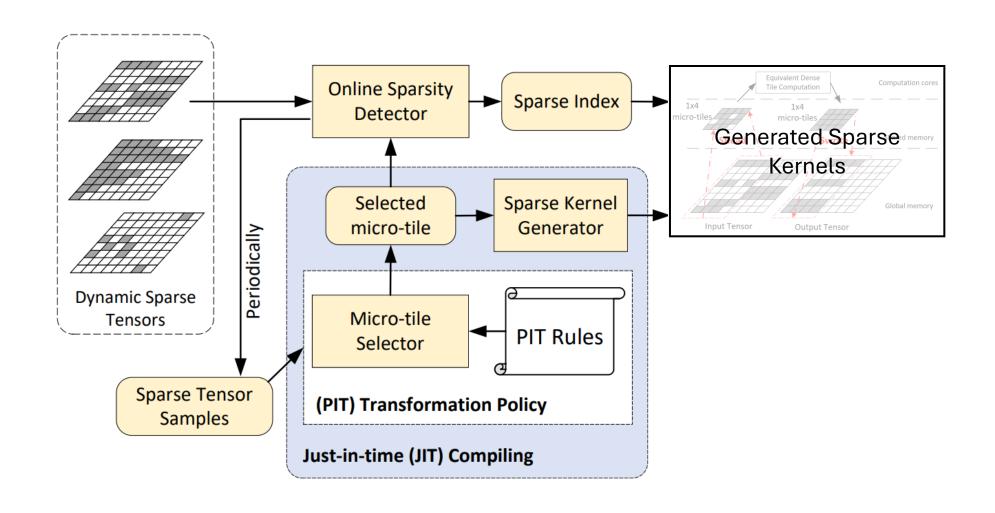


### Online Sparsity Detection and Index Construction

- Minimized construction overhead
  - Constructing index without reformatting the sparse tensor (zero copy)
  - Parallelized index construction in an out-of-order manner thanks to PIT
  - Detecting non-zero values at the granularity of micro-tile



### PIT Online Execution Workflow

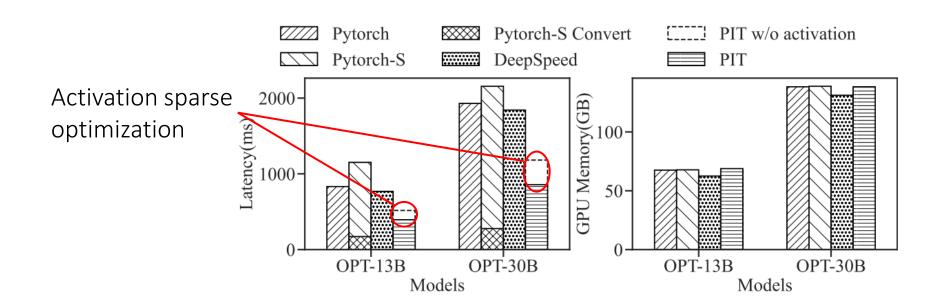


- Comprehensive experiments on popular models, different datasets, precisions, and accelerators
  - Evaluated both inference and training
  - Compared with 6 end-to-end inference libraries
    - PyTorch, PyTorch-S, Tutel, DeepSpeed, MegaBlocks, TurboTransformer
  - Compared with 4 sparse kernel libraries
    - cuSPARSE, OpenAl Triton, Sputnik, SparTA

Models	Datasets	Model Structure	Precision	Devices
Switch Transformers[29]	MNLI [59]	Encoder Decoder MoE	fp16,fp32	A100
Swin-MoE [37]	ImageNet	Encoder MoE	fp16	A100
OPT [66]	Alpaca [58]	Decoder	fp32	V100
BERT [22]	GLUE [59], News [27] etc.	Encoder	fp32	V100
Longformer [14]	Arxiv [21]	Encoder	fp32	V100
MuseFormer [65]	LMD [54]	Decoder	fp32	V100

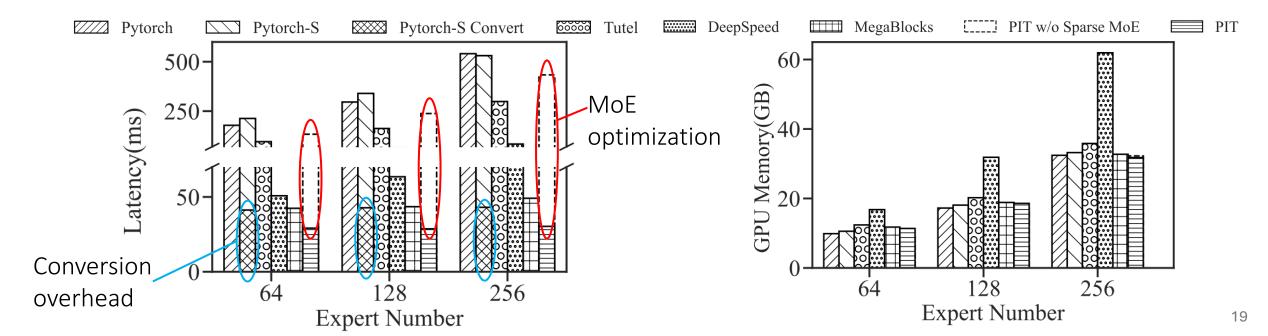
- End-to-End Inference of **OPT** 
  - 8xV100-32GB GPUs
  - FP32 inference latency
  - Batch size is 32

- 2.3x, 2.5x, 2.2x faster over PyTorch, PyTorch-S, DeepSpeed (OPT-30B)
- Gains from varying seq. length and activation sparse
- Memory usage is similar to the baselines



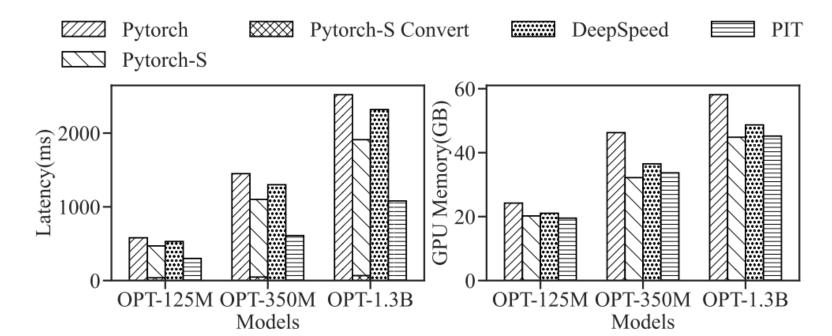
- End-to-End Inference of Switch Transformer (MoE)
  - 1xA100-80GB GPU
  - FP16 inference latency
  - Batch size is 8

- 17.8x, 17.5x, 9.8x, 2.8x, 1.6x faster over PyTorch, PyTorch-S, Tutel, DeepSpeed, MegaBlocks for 256 experts
- Gain comes from MoE and varying seq. length
- Memory usage is low

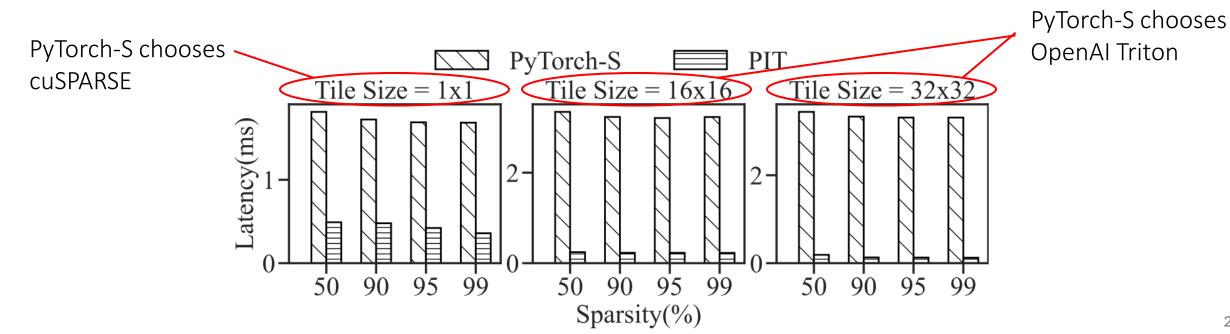


- End-to-End Training of OPT
  - 1xA100-80GB GPU
  - FP32 training speed
  - Batch size is 8 or 4

- 2.3x, 1.8x, 2.1x faster over PyTorch, PyTorch-S, DeepSpeed (OPT-1.3B)
- Gain comes from varying seq. length and sparse attention
- Memory usage is low



- Sparse Index Conversion Overhead
  - 1xV100-32GB GPU
  - Index construction latency of a sparse tensor with shape 4096x4096
  - Gain comes from out-of-order index construction and zero copy of data



#### Conclusion

- PIT demonstrates a novel and effective way of handling dynamic sparsity, a growing trend in deep learning especially LLMs
- With permutation invariant transformation, PIT achieves high computation efficiency, low computation waste, and minimal data conversion overhead
- The idea of decoupling data format and computation logic in PIT can be generalized to other scenarios, e.g., low-bit computation, mixed precisions

#### Conclusion

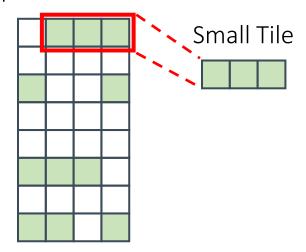
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Q&A

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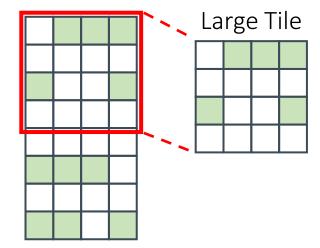
### Inefficiency Due to Dynamic Sparsity

#### Sparse Tensor A



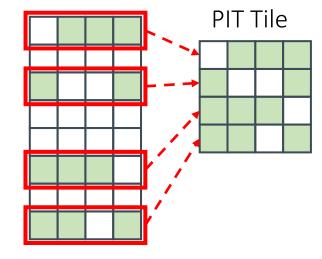
- **V** Low waste
- **×** Low SM Utilization

Sparse Tensor A



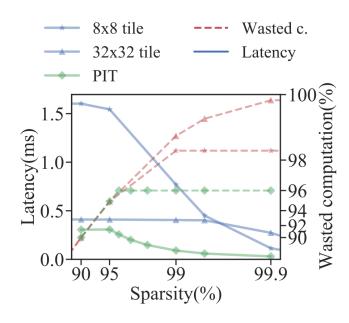
- **∨** High SM Utilization
- × High waste

#### Sparse Tensor A

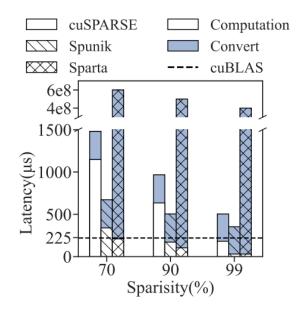


- **∨** High SM Utilization
- **V** Low waste
- **∨** On-the-fly

### Inefficiency Due to Dynamic Sparsity



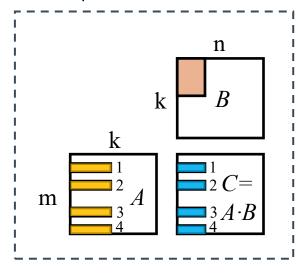
Smaller tiles (e.g., 8x8) have poor performance due to inefficient tile computation though less wasted computation



Sparsity specific kernels requires online data format conversion (e.g., CSR), leading to high overhead

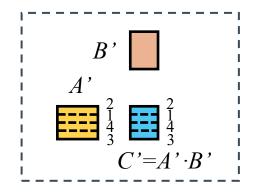
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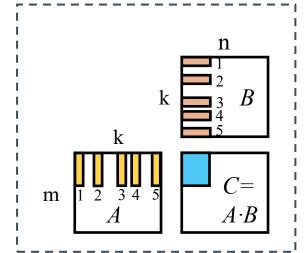
Sparse matrices



Sparse data in A rearranged to dense data A along m-axis







Sparse data in A rearranged to dense data A along k-axis

